$\dot{s} = \bar{\omega}_k + O\left(\frac{\mathbf{u}}{\bar{\omega}_k}\right)$